

Section 2. Energy principle

4. A tennis player wants to toss a 0.057-kg tennis ball into the air so that it rises to a maximum height of exactly 1.7 m. Define the ball to be a “particle” and apply the energy principle to the ball to find the initial speed of the ball, as the ball leaves her hand.
5. While the ball is in her hand, she exerts a constant upward force on the ball as it speeds up from rest to the speed it has when it leaves her hand. If her hand exerts a force on the ball through a displacement of $\langle 0, 0.5, 0 \rangle$ m, what is the force of her hand on the ball?
6. What is the kinetic energy of a proton moving at a speed of $0.9c$? The mass of a proton is 1.7×10^{-27} kg.

Answer Key for Exam A

Section 1. Force of a spring

1. $\vec{F}_{net} = \Delta\vec{p}/\Delta t = 0$
 $\vec{F}_{grav} + \vec{F}_{spring} = 0$
 $\langle 0, ks, 0 \rangle = -\langle 0, -mg, 0 \rangle$
 $k = mg/s$

2. $\vec{F}_{net} = \Delta\vec{p}/\Delta t = 0$
 $\vec{F}_{grav} + \vec{F}_{spring} + \vec{F}_{spring} = 0$
 $\vec{F}_{hand} = -\langle 0, ks, 0 \rangle - \langle 0, -mg, 0 \rangle$
 $\vec{F}_{hand} = \langle 0, mg - ks, 0 \rangle$

3. $A = 0.15m$
 $\omega = \sqrt{k/m} = 7\text{rad/s}$
 $T = 2\pi/\omega = 0.90s$
 $y_0 = A\cos(\phi) = 0.15$ thus, $\phi = 0$
 $y(t) = 0.15\cos(7t)$ m

Section 2. Energy principle

4. $W = \Delta E = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$ for low speeds and no change in rest energy
 $\vec{F}_{grav} \cdot \Delta\vec{r} = -mg\Delta y = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$
 $v_f = \sqrt{2g\Delta y}$

- 5.

6. $K = E - mc^2 = mc^2/\sqrt{1 - v^2/c^2}$