

$$I_0 = 1 \times 10^{-12} \text{ J/s/m}^2$$

Assume a temperature of air such that $v_{\text{sound in air}} = 340 \text{ m/s}$.

Section 1. Multiple Choice

Questions 1-4: A 0.5-kg object hangs from a spring of stiffness 10 N/m. You pull it down 7.5 cm from equilibrium and release it from rest. It oscillates in simple harmonic motion.

1. What is its angular frequency?

- (a) 14.1 rad/s
- (b) 11.5 rad/s
- (c) 1.43 rad/s
- (d) 2.24 rad/s
- (e) 4.47 rad/s**

$$m = 0.5 \text{ kg}$$

$$A = 0.075 \text{ m}$$

$$k = 10 \frac{\text{N}}{\text{m}}$$

$$\omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{10}{0.5}}$$

$$= 4.47 \frac{\text{rad}}{\text{s}}$$

2. What is the total energy of the oscillator?

- (a) 0.028 J**
- (b) 0.38 J
- (c) 0.056 J
- (d) 0.75 J
- (e) 5 J

$$E = \frac{1}{2} k A^2 = \frac{1}{2} (10 \frac{\text{N}}{\text{m}}) (0.075 \text{ m})^2$$

$$= 0.028 \text{ J}$$

3. What is the object's speed when the object is 3 cm from equilibrium?

- (a) 0.13 m/s
- (b) 0.34 m/s
- (c) 0.12 m/s
- (d) 0.053 m/s
- (e) 0.31 m/s**

$$E = \frac{1}{2} k x^2 + \frac{1}{2} m v^2$$

$$\frac{1}{2} m v^2 = E - \frac{1}{2} k x^2$$

$$= 0.0281 \text{ J} - \frac{1}{2} (10) (0.03)^2 = 0.0236 \text{ J}$$

$$v = \sqrt{\frac{2(0.0236 \text{ J})}{0.5 \text{ kg}}}$$

$$= 0.307 \frac{\text{m}}{\text{s}}$$

4. If you repeat the experiment but pull it down a total of 2 cm from equilibrium and release it from rest, the angular frequency is

- (a) greater than the previous experiment.
- (b) less than the previous experiment.
- (c) the same as the previous experiment.**

ω does not depend on A

5. Spring A has twice the stiffness of Spring B. If the same mass is attached to each spring and oscillates, the angular frequency of Spring A is

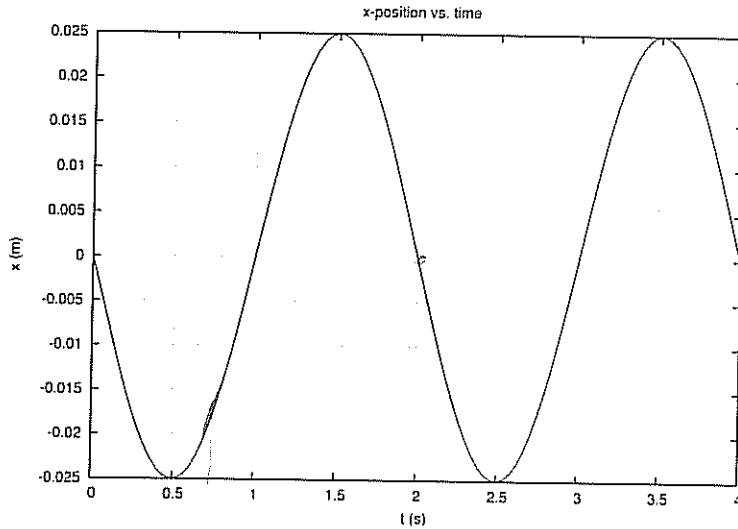
- (a) $(1/\sqrt{2})\omega_B$
- (b) $(1/2)\omega_B$
- (c) $2\omega_B$
- (d) $\sqrt{2}\omega_B$**
- (e) equal to ω_B .

$$\omega = \sqrt{\frac{k}{m}} \quad k_A = 2k_B$$

$$\omega_A = \sqrt{\frac{2k_B}{m}} = \sqrt{2} \sqrt{\frac{k_B}{m}}$$

$$= \sqrt{2} \omega_B$$

Questions 6-8: A 0.25 kg object oscillates on a spring in simple harmonic motion. The graph of $x(t)$ is shown below.



6. What is its frequency?

- (a) 0.67 Hz
- (b) 40 Hz
- (c) 0.5 Hz
- (d) 0.29 Hz
- (e) 1.0 Hz

$$T = 2 \text{ s}$$

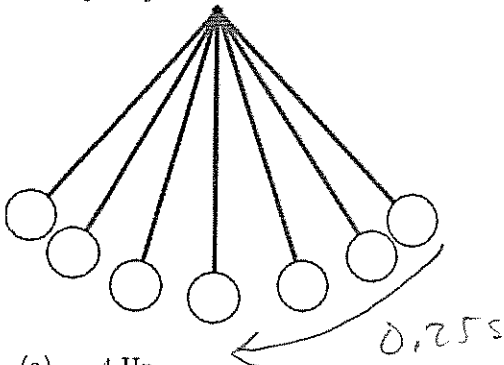
$$f = \frac{1}{T} = \frac{1}{2 \text{ s}} = 0.5 \text{ Hz}$$

7. The x -velocity at $t = 0.7 \text{ s}$ is

- (a) positive
- (b) negative
- (c) zero

v_x is slope and is pos. / pos. slope.

8. A pendulum swings back and forth in simple harmonic motion as shown below. It takes 0.25 s to swing from its furthest point on the right to the equilibrium position while it is oscillating. What is its frequency?



- (a) 4 Hz
- (b) 2 Hz
- (c) 1 Hz
- (d) 0.5 Hz
- (e) 0.25 Hz

$\frac{1}{4}$ oscillation in 0.25 s

so $T = 1 \text{ s}$

$$f = \frac{1}{T} = 1 \text{ Hz}$$

9. A simple harmonic oscillator consists of a 0.5 kg mass on a spring of stiffness 8 N/m. If you pull it back 0.05 m from equilibrium and release it from rest, what will be its maximum speed?

- (a) 0.80 m/s
- (b) 0.20 m/s
- (c) 0.89 m/s
- (d) 0.63 m/s
- (e) 0.40 m/s

$$E_i = E_f$$

$$\frac{1}{2}kA^2 = \frac{1}{2}mv_{max}^2$$

$$v_{max} = \sqrt{\frac{k}{m}} A = \sqrt{\frac{8}{0.5}} (0.05m) = 0.2 \frac{m}{s}$$

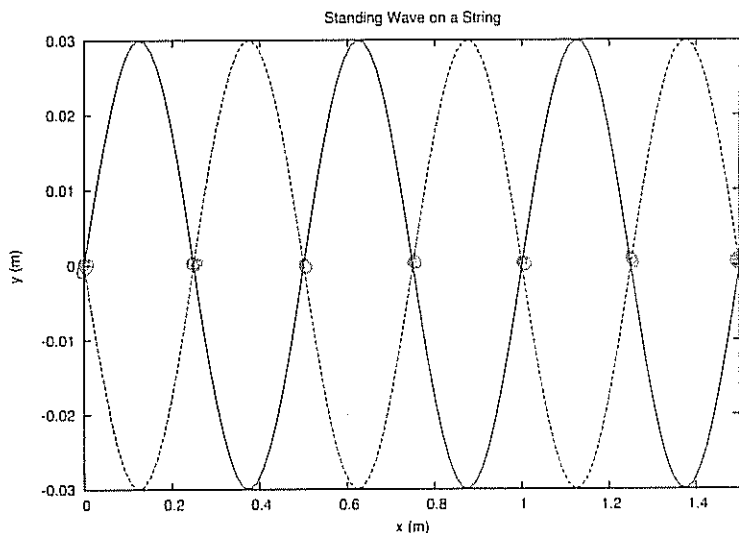
10. For the oscillator in the previous question, if you triple its amplitude by pulling it back 0.15 m when you release it from rest, the total energy of the oscillator will increase by a factor of

- (a) 3
- (b) 4
- (c) 6
- (d) 9
- (e) none of the above, because the total energy will be the same

$$E \propto A^2$$

$$(3A)^2 = 9A^2 \text{ so } E \text{ increases by } 9.$$

Questions 11–13: Suppose that in a particular experiment, you create a standing wave on a string that looks like the picture shown below.



11. How many nodes are there?

- (a) 6
- (b) 12
- (c) 3
- (d) 14
- (e) 7

7 nodes

12. What is the wavelength?

- (a) 0.25 m
- (b) 0.21 m
- (c) 1.5 m
- (d) 0.75 m
- (e) 0.5 m

$$L = 1.5m$$

3λ are shown, so

$$3\lambda = L$$

$$\lambda = \frac{L}{3} = 0.5m$$

13. For the previous question, suppose that you want a standing wave that is a higher harmonic. What should you do to the tension in the string (assuming that the frequency and length stay the same)?

- (a) increase the tension
- (b) decrease the tension
- (c) none of the above because changing the tension will not change the harmonic of the standing wave

$$v = \lambda f = \frac{2L}{n} f \quad \mu = \frac{2Lf}{2v} \quad \text{need lower } v, \text{ so lower tension.}$$

14. String Y is thicker than String Z, but they are both made of the same material. Which guitar string will have a higher fundamental frequency?

- (a) String Y
- (b) String Z
- (c) Neither because they will both have the same fundamental frequency.

$$f = \frac{2L}{n} v = \frac{2L}{n} \sqrt{\frac{F}{\mu}} \quad f \propto \frac{1}{\sqrt{\mu}} \quad \mu_Y > \mu_Z \text{ so } f_Y < f_Z$$

15. For a standing wave in a pipe that is closed at one end, the displacement of the air at the closed end is

- (a) neither a node nor an antinode.
- (b) either a node or antinode depending on the wavelength of the standing wave.
- (c) an antinode.
- (d) a node.

air cannot oscillate at the closed end.

16. Sound is a

- (a) longitudinal wave
- (b) transverse wave
- (c) neither of the above because it can be both a longitudinal and a transverse wave

17. A pipe has a closed end and an open end. For air in the pipe ($v = 340 \text{ m/s}$), what is the frequency of the fundamental if the length of the pipe is 0.1 m ?

- (a) 680 Hz
- (b) 1700 Hz
- (c) 425 Hz
- (d) 850 Hz
- (e) 1133 Hz

$$f = \frac{v}{4L} = \frac{340 \text{ m/s}}{4(0.1 \text{ m})} = 850 \text{ Hz}$$

18. Which will have a fundamental frequency that is lower, a pipe that is (a) open at one end and closed at the other or (b) a pipe that is open at both ends? (Assume that all other characteristics are identical.)

- (a) The pipe that is closed at one end and open at the other.
- (b) The pipe that is open at both ends.
- (c) Neither, because they will have the same fundamental frequency.

$$\text{open-open } f = \frac{1}{2L} v$$

$$\text{open-closed } f = \frac{1}{4L} v$$

19. Suppose that when listening to music normally in the car, the sound level is 80 dB . However, your friend with the super-cool, shake-the-car speakers turns it up to 110 dB . By what factor did he increase the intensity of the sound?

- (a) 10
- (b) 100
- (c) 110
- (d) 1,000
- (e) 10,000

$$\text{Sound level} = 10 \text{ dB } \log\left(\frac{I}{I_0}\right)$$

$$\text{If } \frac{I}{I_0} = 10, \text{ level} = 10 \text{ dB}$$

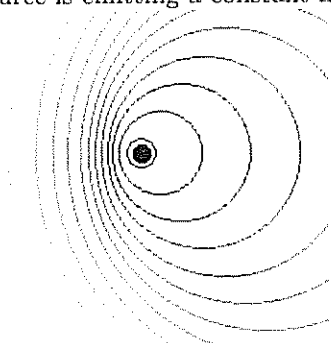
$$\frac{I}{I_0} = 100, \text{ level} = 20 \text{ dB}$$

$$\frac{I}{I_0} = 1000, \text{ level} = 30 \text{ dB}$$

an increase in 10 dB is a factor of 10 increase in intensity

$0 \text{ dB} - 80 \text{ dB} = 30 \text{ dB}$
 so 3 factors of 10 or 10^3

20. A source is emitting a constant frequency sound wave in all directions as it moves, as shown below.



In what direction is the source traveling?

- (a) to the right
- (b) to the left *wave crests are closer together*
- (c) Neither because the source is stationary.
- (d) There is not enough information from the picture to answer the question.

21. A pedestrian standing at the curb hears the horn of a car approaching her at 26 m/s. She hears a frequency of 600 Hz. At what frequency does the driver in the car hear the horn? (Use a speed of $v = 340$ m/s for sound in the air at this temperature).

- (a) 646 Hz
- (b) 600 Hz
- (c) 574 Hz
- (d) 626 Hz
- (e) 554 Hz

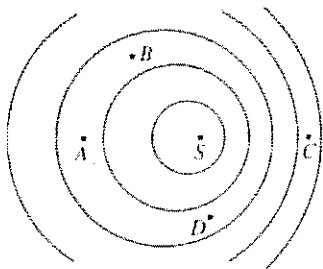
$$f_d = \left(\frac{v + v_d}{v - v_s} \right) f_s$$

$$f_s = \frac{v - v_s}{v + v_d} f_d = \left(\frac{340 - 26}{340} \right) (600)$$

$$= \boxed{554 \text{ Hz}}$$

Handwritten notes:
 $f_d = 600 \text{ Hz}$
 $f_s = ?$
 $v_s = 26 \frac{\text{m}}{\text{s}}$
 $v_d = 0$
 $v = 340 \frac{\text{m}}{\text{s}}$

22. A source is emitting a constant frequency sound wave in all directions as it moves, as shown below.

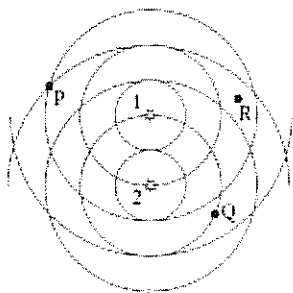


At which of the labeled points will the frequency measured by a stationary listener be greatest?

- (a) A
- (b) B
- (c) C
- (d) D
- (e) It will be the same for all four points.

Handwritten notes:
 $v = \lambda f$ large f is small λ .
 (or "short" λ)

23. Two identical sources emit waves of wavelength λ shown below.

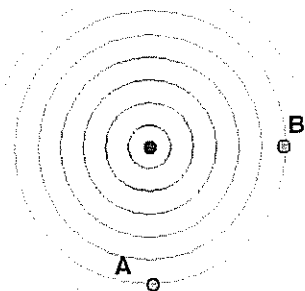


*R is at a crest for source 1
and a crest for source 2.
const. interference*

At point R, the interference of the waves from the two sources is

- (a) constructive
- (b) destructive
- (c) There's not enough information to determine the interference.

24. A point source of sound waves is shown below. Person A stands at location A and holds a microphone with a circular area of 1 cm^2 . Person B stands at location B and holds a microphone with a circular area of 2 cm^2 . At which microphone is the intensity of the sound the greatest?



*distance to each point is the
same so I is the
same*

- (a) A
- (b) B
- (c) The intensity is the same at the location of each microphone.

25. Which microphone absorbs the greatest amount of energy per second?

- (a) A
- (b) B
- (c) The microphones absorb the same amount of energy per second.

$$A_B > A_A$$

$$P = IA$$

*So larger area mic absorbs more
energy.*