

Unless otherwise stated, use a coordinate system with  $+x$  to the right and  $+y$  upward, toward the top edge of the page.

Section 1.

Questions 1-2: Copper has a density of  $8960 \text{ kg/m}^3$  and an atomic mass of  $63.55 \text{ g/mol}$ . One atom of copper has 29 protons and 29 electrons. Avogadro's number is  $6.02 \times 10^{23} \text{ atoms/mol}$ . A certain copper BB has a volume  $5.00 \times 10^{-10} \text{ m}^3$ .

1. How many electrons are in the BB?

- (a)  $1.23 \times 10^{21}$  electrons
- (b)  $4.24 \times 10^{19}$  electrons
- (c)  $2.46 \times 10^{19}$  electrons
- (d)  $2.70 \times 10^{18}$  electrons
- (e)  $7.82 \times 10^{19}$  electrons

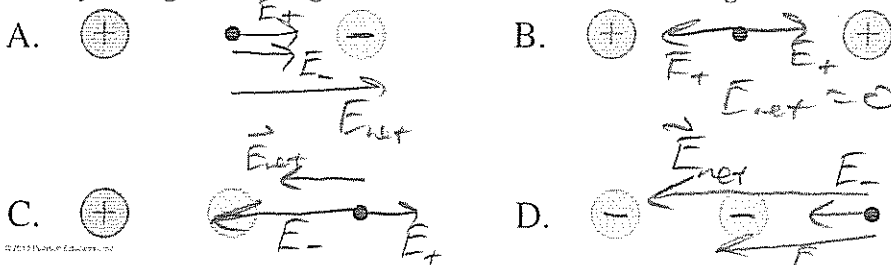
$$\left( \frac{8960 \text{ kg}}{\text{m}^3} \right) \left( 5 \times 10^{-10} \text{ m}^3 \right) \left( \frac{1 \text{ mol}}{0.06355 \text{ kg}} \right) \left( 6.02 \times 10^{23} \frac{\text{atoms}}{\text{mol}} \right) = 4.24 \times 10^{19} \text{ atoms} \left( \frac{29 \text{ elect}}{\text{atom}} \right) = 1.23 \times 10^{21} \text{ elect.}$$

2. If the BB has an electric charge of  $-2 \text{ nC}$ , how many additional electrons did it gain?

- (a)  $3.2 \times 10^{28}$  electrons
- (b)  $1.25 \times 10^{10}$  electrons
- (c)  $1.25 \times 10^{19}$  electrons
- (d)  $2.0 \times 10^9$  electrons
- (e)  $8.0 \times 10^{11}$  electrons

$$(-2 \times 10^{-9} \text{ C}) \left( \frac{1 \text{ elect.}}{-1.6 \times 10^{-19} \text{ C}} \right) = 1.25 \times 10^{10} \text{ elect.}$$

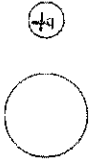
3. Two equal magnitude charges are shown in four different configurations.



In which case(s) does the net electric field at the dot point to the left.

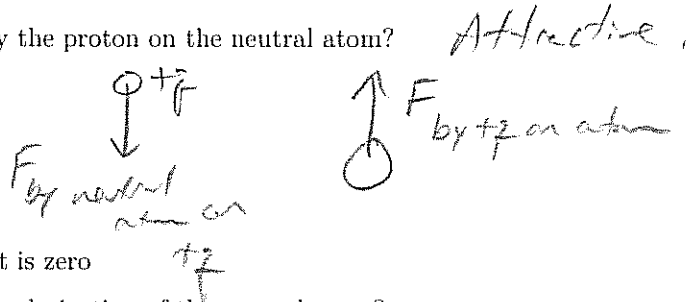
- (a) A only
- (b) D only
- (c) C only
- (d) C and D
- (e) A, C, and D

Questions 4-5: A proton  $+q$  is near a neutral atom (the circle) as shown below.

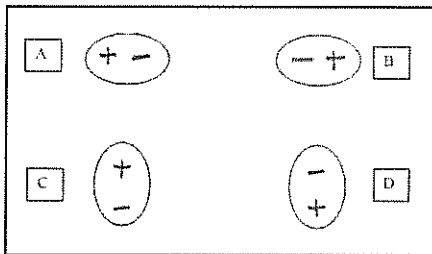


4. What is the direction of the force by the proton on the neutral atom?

- (a) to the right,  $+x$
- (b) to the left,  $-x$
- (c) upward,  $+y$
- (d) downward,  $-y$
- (e) none of the above because it is zero



5. Which of these diagrams shows the polarization of the neutral atom?



*electron cloud attracted to +q.*

- (a) A
- (b) B
- (c) C
- (d) D

Questions 6-8: You have four metal disks with charges:  $q_A = -8.0 \mu\text{C}$ ,  $q_B = -2.0 \mu\text{C}$ ,  $q_C = +5.0 \mu\text{C}$ , and  $q_D = +12.0 \mu\text{C}$ .

6. Holding them with insulators, you bring two disks together so that they touch. Then you separate them. You measure the resulting charge of each disk and find that it is  $+5.0 \mu\text{C}$  per disk. Which two disks did you bring together?

- (a) A and B
- (b) B and C
- (c) C and D
- (d) B and D
- (e) A and D

$Q_{\text{total}} = +5 + 5 = 10 \mu\text{C}$ .  
 Before touching  $Q_{\text{total}} = 10 \mu\text{C}$ . So  
 disks are B and D since

7. If you touch disk A and disk B together,

- (a) A will gain electrons
- (b) A will gain protons
- (c) A will lose electrons
- (d) A will lose protons

$q_B + q_D = -2 + 12 = 10 \mu\text{C}$

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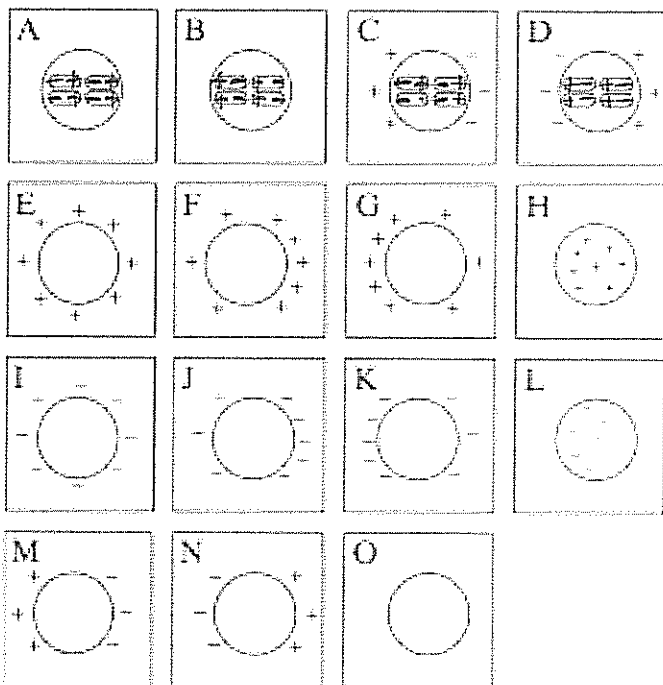
A loses neg. charge so it  
 loses electrons.

8. If you touch disk C and disk D together,

- (a) C will gain electrons
- (b) C will gain protons
- (c) C will lose electrons
- (d) C will lose protons

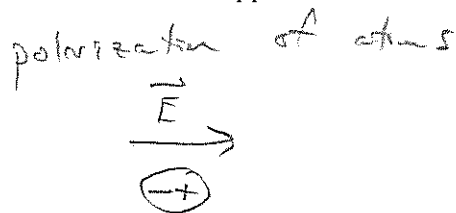
*C gains + charge. The only way for a conductor to do this is to lose electrons.*

Questions 9-10: Use this image to answer each of the following questions.



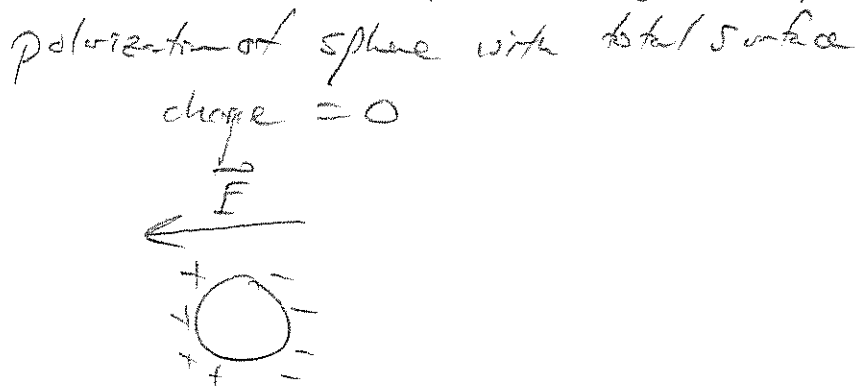
9. Which sphere is a neutral insulator in an applied electric field (due to other charges not shown) that is to the right?

- (a) A
- (b) B
- (c) C
- (d) D
- (e) O



10. Which sphere is a neutral conductor in an applied electric field (due to other charges not shown) that is to the left?

- (a) M
- (b) N
- (c) C
- (d) D
- (e) O



Questions 11–13: Three charged spheres are arranged as shown below. In the figure,  $d = 4 \text{ cm}$  and  $q = 1 \mu\text{C}$ .



11. What is the magnitude of the force by the particle of charge  $-2q$  on the particle of charge  $-q$ ?

- (a) 5.6 N
- (b) 0.45 N
- (c) 2.8 N
- (d) 22 N
- (e) 11 N

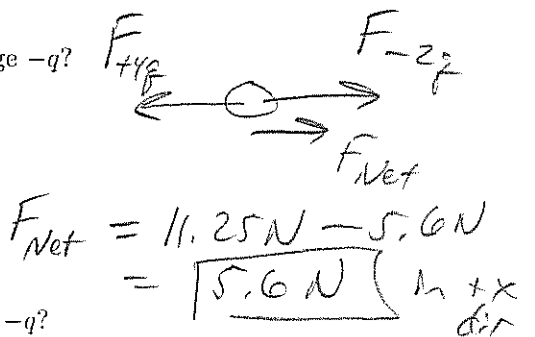
$$F = \frac{(9 \times 10^9)(2)(1 \times 10^{-6})(1 \times 10^{-6})}{(0.04 \text{ m})^2} = 11.25 \text{ N}$$

$\leftarrow F_{-2q}$

12. What is the magnitude of the net force on the particle of charge  $-q$ ?

- (a) zero
- (b) 17 N
- (c) 11 N
- (d) 22 N
- (e) 5.6 N

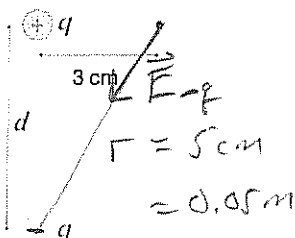
$$F_{4q} = \frac{(9 \times 10^9)(4)(1 \times 10^{-6})(1 \times 10^{-6})}{(0.08)^2} = 5.6 \text{ N in } -x \text{ dir.}$$



13. What is the direction of the net force on the particle of charge  $-q$ ?

- (a) to the right,  $+x$
- (b) to the left,  $-x$
- (c) none of the above because it is zero

Questions 14–16: A dipole made of charged spheres with  $q = 8 \text{ nC}$ ,  $d = 4 \text{ cm}$  is shown below?



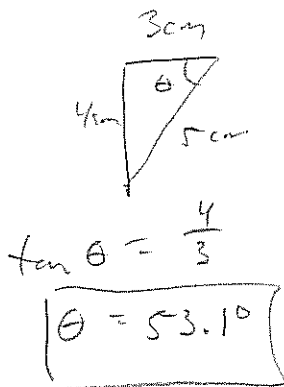
14. What is the magnitude of the electric field due to  $-q$  at the location of the dot?

- (a) 45,000 N/C
- (b) 80,000 N/C
- (c) 57,600 N/C
- (d) 90,000 N/C
- (e) 28,800 N/C

$$E = \frac{(9 \times 10^9)(8 \times 10^{-9} \text{ C})}{(0.05 \text{ m})^2} = 28,800 \frac{\text{N}}{\text{C}}$$

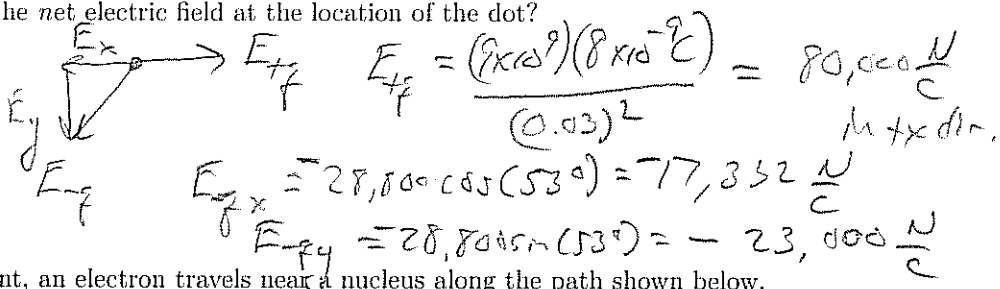
15. What is the angle with respect to the horizontal for the electric field due to  $-q$  at the location of the dot?

- (a)  $37^\circ$
- (b)  $45^\circ$
- (c)  $30^\circ$
- (d)  $53^\circ$
- (e)  $60^\circ$

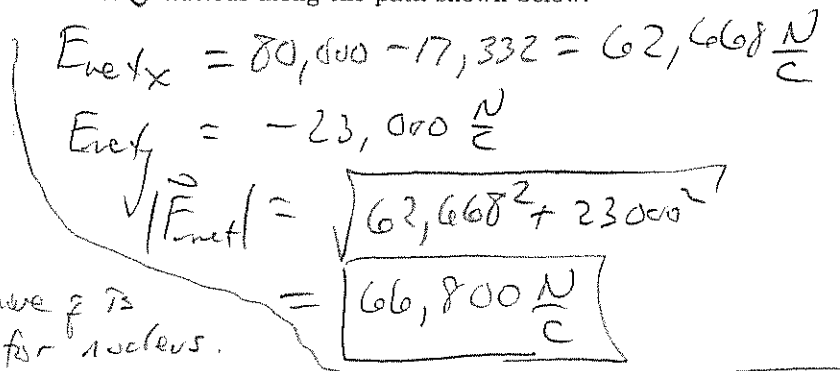
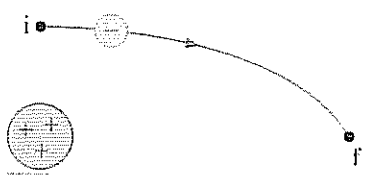


16. What is the magnitude of the net electric field at the location of the dot?

- (a) 97,300 N/C
- (b) 109,000 N/C
- (c) 98,600 N/C
- (d) 120,000 N/C
- (e) 100,000 N/C



Questions 17-19: In an experiment, an electron travels near a nucleus along the path shown below.



17. The potential difference,  $\Delta V = V_f - V_i$ , is

- (a) positive.
- (b) negative.
- (c) zero.

$V = \frac{q_2 q_1}{r}$  where  $q$  is for nucleus.  
 So  $V_f < V_i$  and  $\Delta V$  is -.

18. As the electron travels from  $i$  to  $f$ , the potential energy,  $U$ , of the system (of electron and nucleus)

- (a) increases.
- (b) decreases.
- (c) remains constant.

$U = qV = -eV$

$U_f$  is a smaller - number than  $U_i$  so  $U$  increases.

19. As it travels from  $i$  to  $f$ , the kinetic energy of the electron

- (a) increases.
- (b) decreases.
- (c) remains constant.

$\Delta U$  is + so

$\Delta K$  is -. Electron slows down

Questions 20-21: In a particular LEGO kit, a capacitor with a capacitance of 0.5 F is charged by a solar cell. The solar cell produces a potential difference of 4 V across the capacitor. The area of each plate is 0.01 m<sup>2</sup> and they are separated 0.1 mm.

20. How much charge is stored on each capacitor plate?

- (a) 0.125 C
- (b) 0.5 C
- (c) 2.0 C
- (d) 8.0 C
- (e) 4.0 C

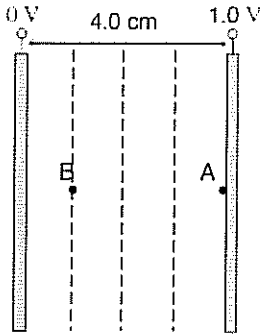
$Q = C \Delta V$   
 $= (0.5 F)(4 V)$   
 $= 2 C$

21. What is the dielectric constant  $K$  of the insulator that is between the plates?

- (a)  $1.1 \times 10^{13}$
- (b)  $2.3 \times 10^9$
- (c)  $4.5 \times 10^9$
- (d)  $1.1 \times 10^9$
- (e)  $5.6 \times 10^8$

$C = \frac{K \epsilon_0 A}{d}$  so  $K = \frac{Cd}{\epsilon_0 A}$   
 $= \frac{(0.5 F)(0.1 \times 10^{-3} m)}{(8.85 \times 10^{-12})(0.01 m^2)}$   
 $= 5.6 \times 10^8$

Questions 22–25: Two electrodes, shown below, are connected to a battery with a potential difference of 1 V. The dotted lines are 1 cm apart.



22. What is the magnitude of the electric field between the plates?

- (a) 4 V/m
- (b) 50 V/m
- (c) 25 V/m
- (d) 100 V/m

$$|\Delta V| = Ed$$

$$E = \frac{1V}{0.04m} = 25 \frac{V}{m}$$

23. What is the direction of the electric field between the plates?

- (a) to the right
- (b) to the left
- (c) upward
- (d) downward
- (e) none of the above because it is zero

$$\leftarrow \vec{E} \text{ toward lower } V.$$

24. What is the electric potential  $V$  at point B?

- (a) 0 V
- (b) 0.25 V
- (c) 0.5 V
- (d) 0.75 V
- (e) 1.0 V

$$V_B - V_A = -E(x_B - x_A)$$

$$V_B - 1 = -(-25 \frac{V}{m})(-0.03m)$$

$$= 1 - 0.75 V = \boxed{0.25 V}$$

Note that  $V$  increases linearly from 0 to 1V. Since B is  $\frac{1}{4}$  the distance, it's  $\frac{1}{4}$  the voltage.

25. If an electron travels from point A to point B, what is its change in electric potential energy,  $\Delta U$ , in eV?

- (a) 0
- (b) 0.25 eV
- (c) 0.5 eV
- (d) 0.75 eV
- (e) 1.0 eV

$$\Delta U = q \Delta V$$

$$U_f - U_i = q(V_f - V_i)$$

$$= -e(V_f - V_i)$$

$$= -e(0.25V - 1V)$$

$$= e(0.75V)$$

$$= \boxed{0.75 eV}$$